

# Shock Wave Induced Damage in Soft Tissue



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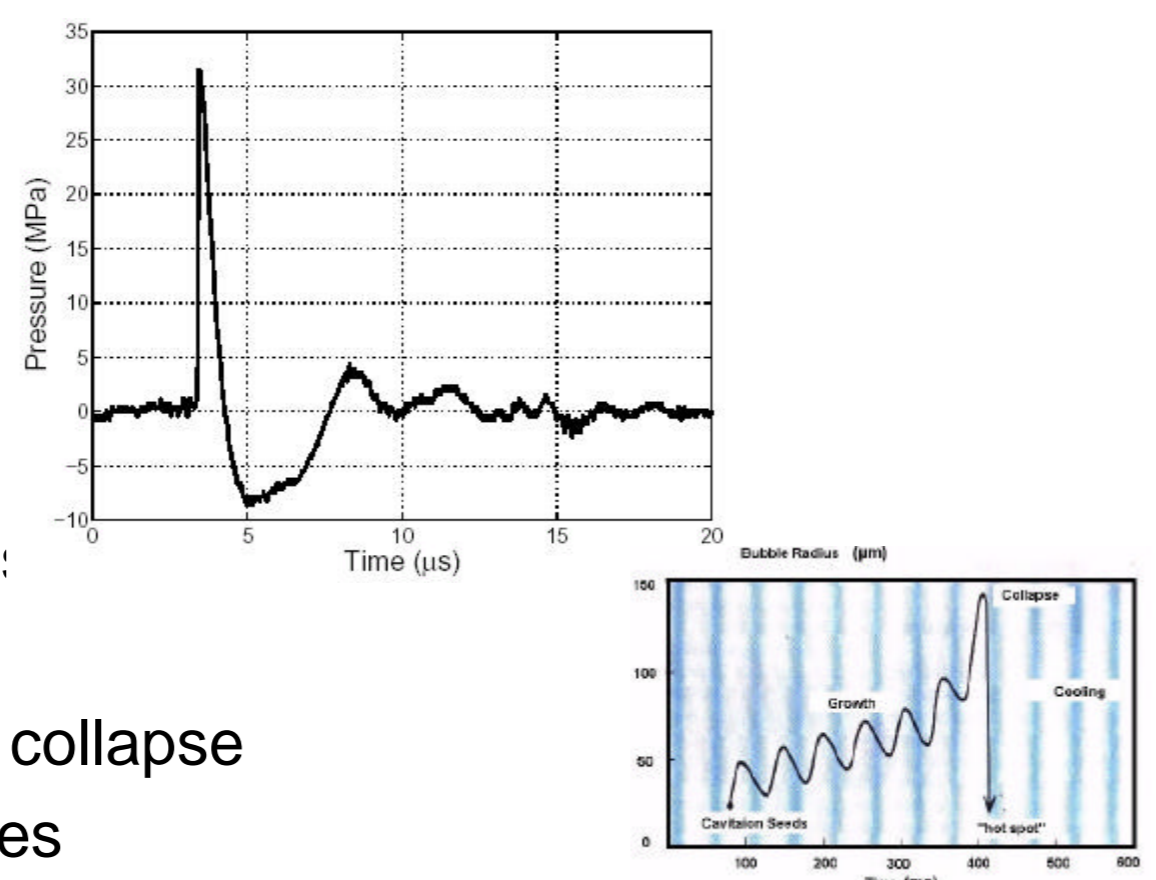


## Problem: Shock-Wave Lithotripsy (SWL)

In SWL, a very common, non-invasive method to destroy kidney stones, the kidney is blasted with high intensity sound waves generated outside the patient and focused on the stone.

focused (direct) shock waves:

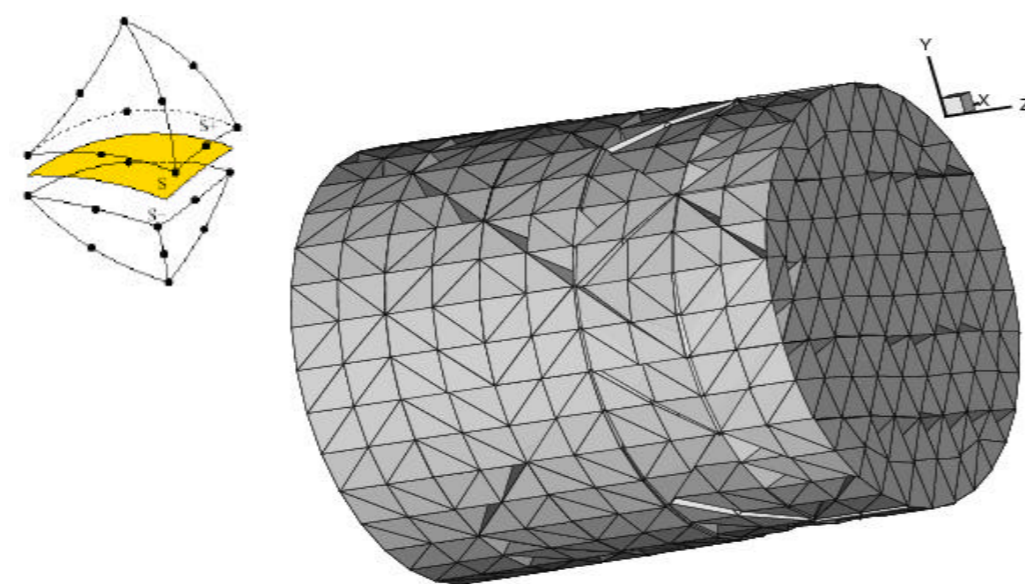
- compression induced cracks
- stone spallation by reflection
- tissue shearing
- tension “tail” of the pressure impul:



indirect shock waves:

- cavitation - bubble expansion and collapse
- pitting by “jets” of collapsing bubbles
- tension waves by reflection – dilatation of vessels and capillaries

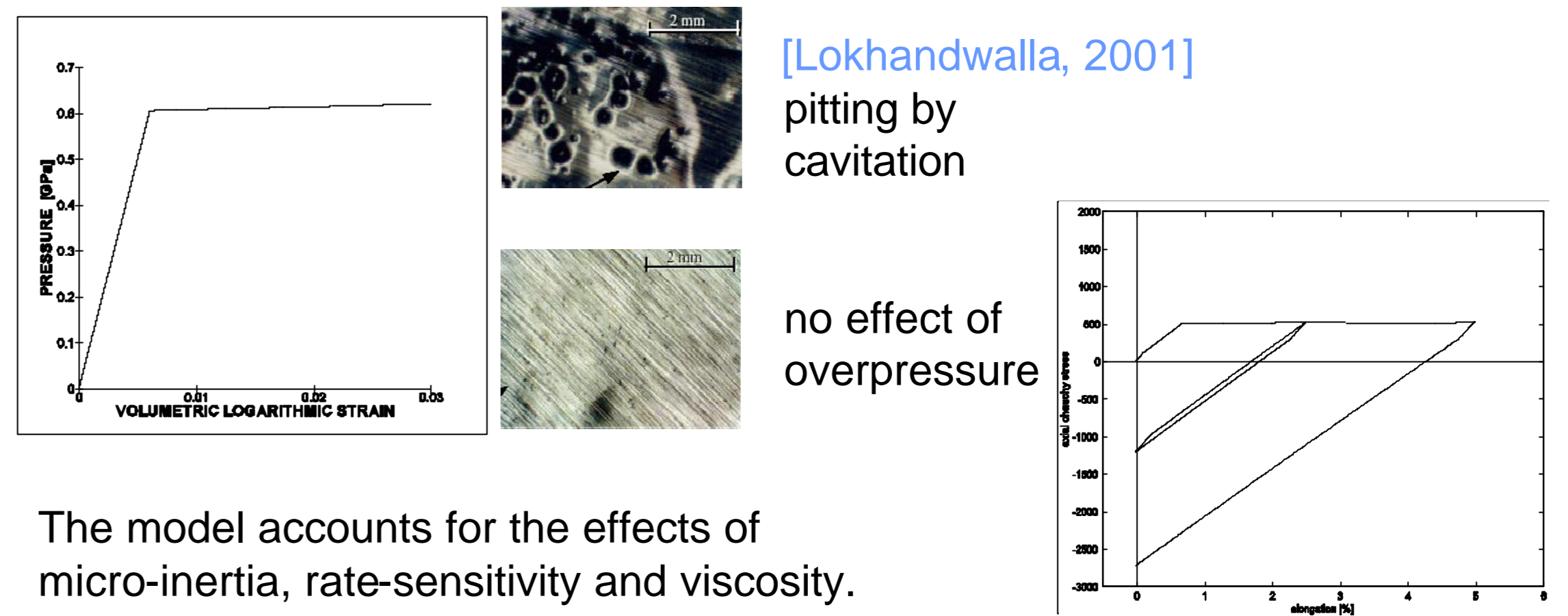
Our numerical simulations of stone spallation use a fragmentation technique of [Pandolfi & Ortiz, 2002] with special cohesive elements.



Journal of Urology (1992):  
 “SWL is a form of renal trauma”

Shock waves focus at stone but damage tissue!

In tension the hydrostatic pressure  $s$  bounded by a critical cavitation pressure  $p = p(E, v, s_p, t, \dots)$ , in compression the material is pressure insensitive.



[Lokhandwalla, 2001]

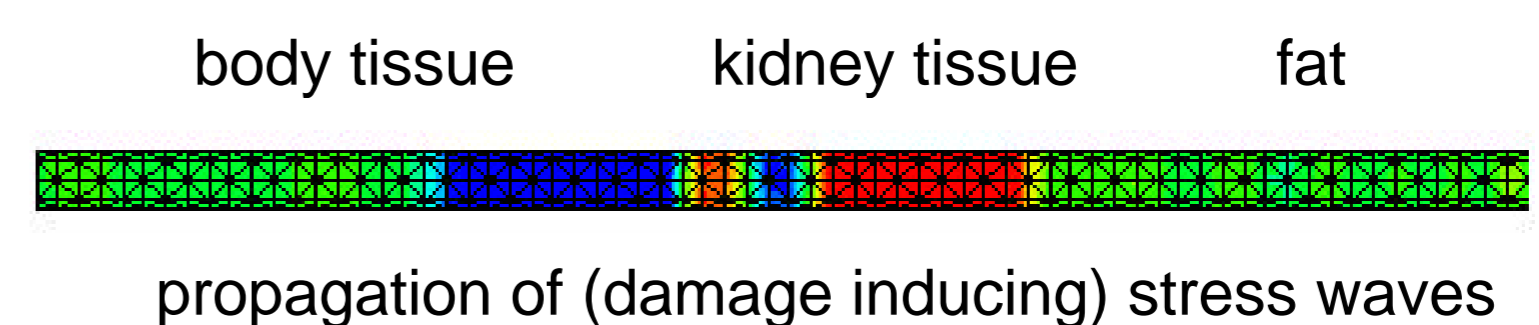
pitting by cavitation

no effect of overpressure

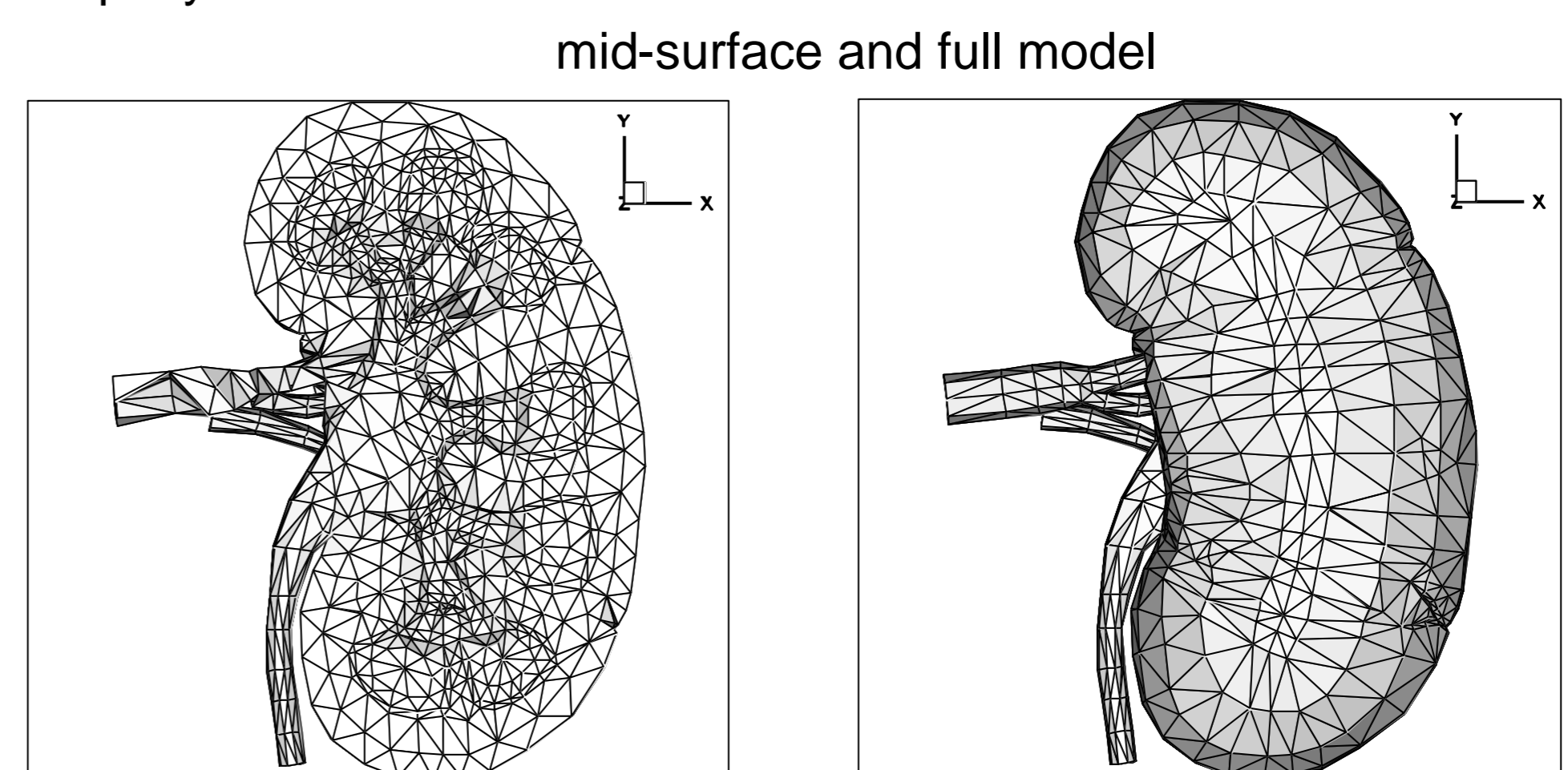
The model accounts for the effects of micro-inertia, rate-sensitivity and viscosity.

## Numerical Simulation

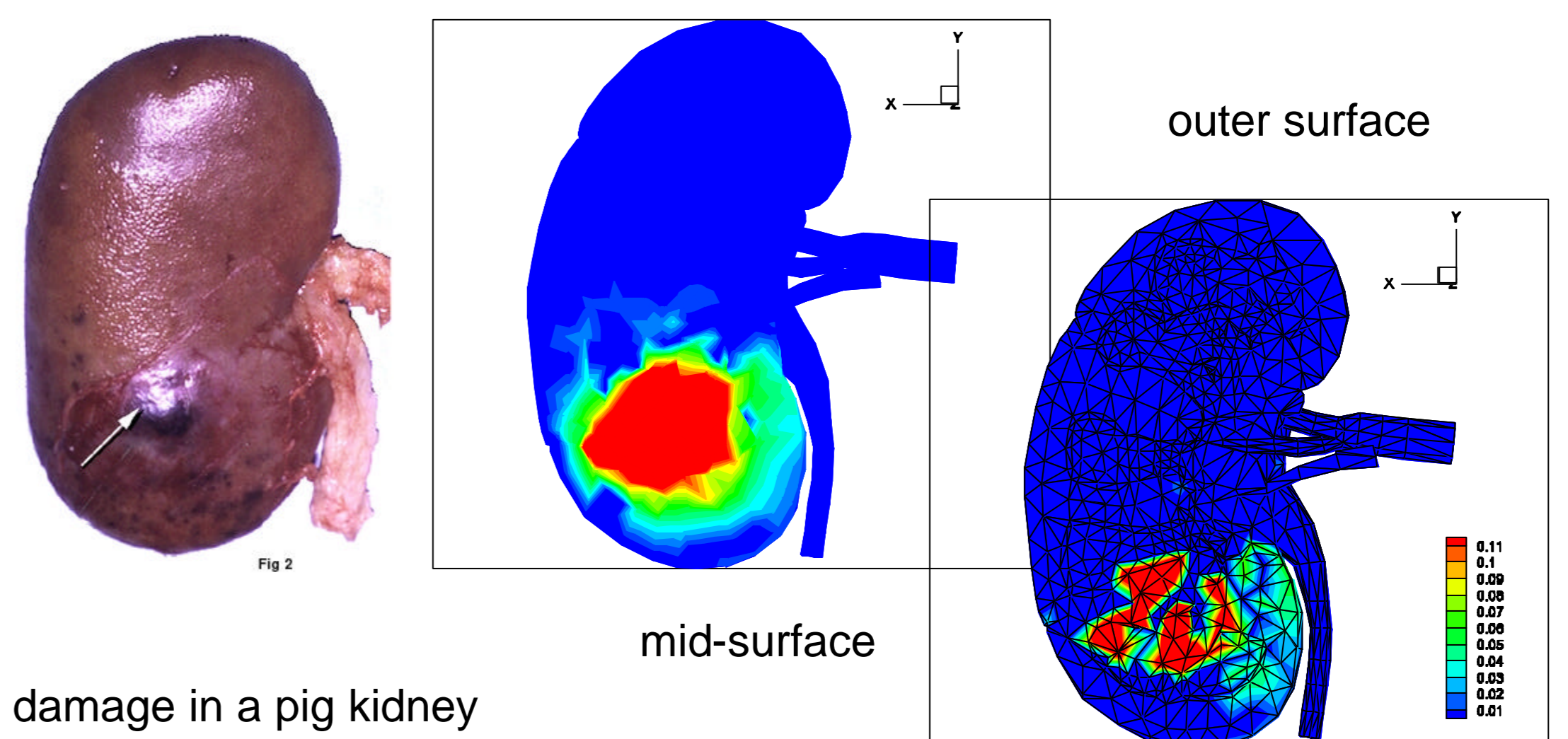
- Elastic material data (elastic modulus 0.05 ... 0.3 MPa, viscosity 0.001 ... 0.007 Pa s) are known, but only few experiments determine inelastic properties.
- Different parameters for different regions of the kidney are not available, all data are homogenized for “the kidney”.
- Parametric studies on the effect of varying material data (uniaxial strain):



- First finite element mesh bases on geometrical data purchased from a company.



- functional tissue (renal cortex, medulla, ...) : new material model
- non-functional tissue (ureter, main arteries and veins): non-linear elastic material



- damage in a pig kidney experiments by [Cleveland et al., 2000]
- color: irreversible volumetric expansion (damage)

## Material Model: Kidney Tissue

The elastic behavior of the soft tissue is constrained by a deviatoric stress measure corresponding to a shear stress.

logarithmic plastic strain:  $\mathbf{e}^p$

The volumetric expansion of the body  $V = JV_0$  with  $J = J^e J^p = \det(\mathbf{F})$  is induced by hydrostatic tension.

logarithmic plastic dilatation:  $\mathbf{J}^p$

The tissue material is incompressible, irreversible volumetric expansion is only induced by cavitation of (empty) bubbles.

$$\frac{d}{dt} \frac{4p}{3} (r^3 - a^3) = 0 \rightarrow \dot{\mathbf{e}}^p = \frac{\partial \dot{r}}{\partial r}$$

The diagram shows a bubble with an outer radius  $r$  and an inner cavity of radius  $a$ . Arrows indicate the expansion of the bubble.

Formulate the corresponding energy of dissipated volumetric work and the kinetic energy of expanding bubbles as a function of radius, expansion velocity and cavity size distribution.

The plastic dilatation relates to micro-mechanic via the volume of the cavities, e.g., for  $N$  cavities with radius  $a$  :

$$\mathbf{J}^p = \log \left( 1 + \frac{4}{3} p N (a^3 - a_0^3) \right)$$

Use an incremental solution procedure and define in every time interval an update-energy function in terms of logarithmic plastic variables.

$$f_n(\mathbf{F}_{n+1}, \mathbf{e}_{n+1}^p, \mathbf{M}, \mathbf{q}_{n+1}^p) = W^e(\mathbf{F}_{n+1}^e, \mathbf{J}_{n+1}^p) + W^p(\mathbf{e}_{n+1}^p, \mathbf{J}_{n+1}^p) + K(\mathbf{J}_{n+1}^p, \mathbf{J}_{n+1}^p) + \Delta t \mathbf{y}^* (\Delta \mathbf{J}^p, \Delta \mathbf{e}^p, \Delta t)$$

Compute the updated internal variables by:  $W_n = \min_{\mathbf{e}_{n+1}^p, \mathbf{M}, \mathbf{J}_{n+1}^p} f_n$