



# Measurement Methods for Single- and Multi-Component Gas Adsorption Equilibria

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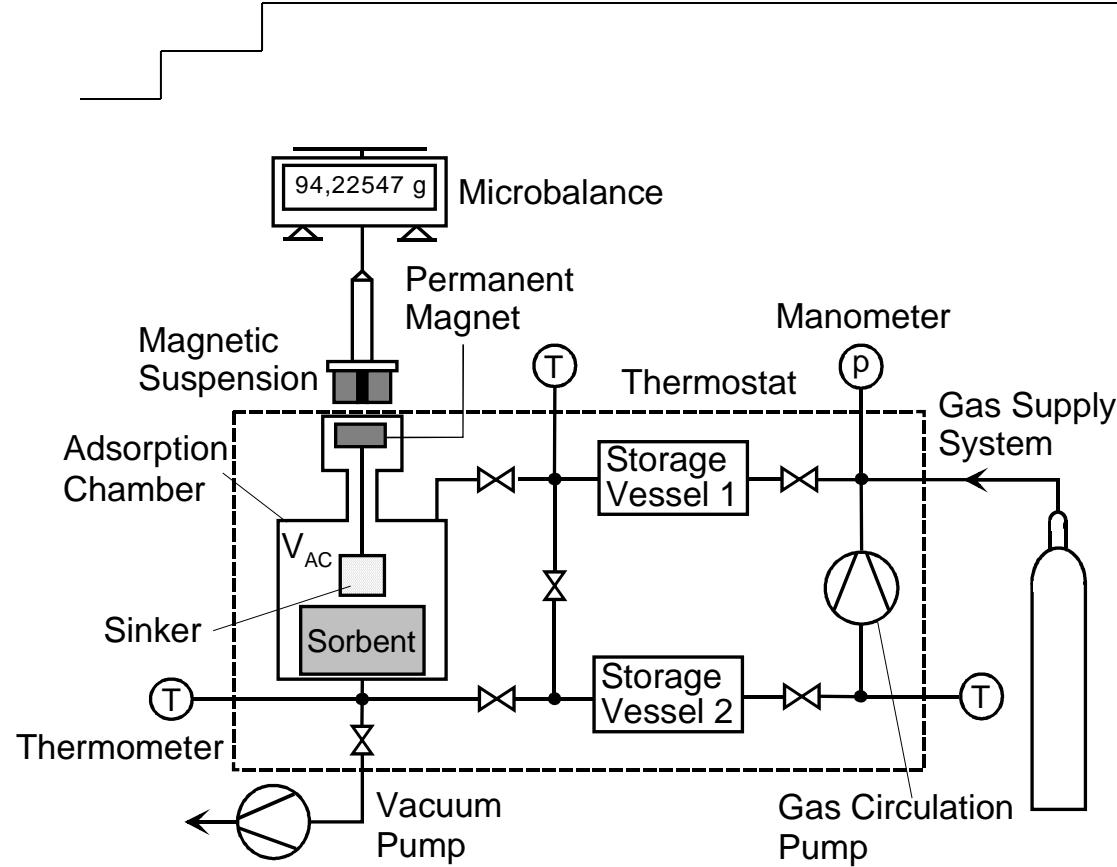
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1. Volumetry / Manometry and Densimetry
  2. Gravimetry and Densimetry
  3. Oscillometry
  4. Impedance Spectroscopy
  5. Calorimetry and Volumetry
  6. Calorimetry and Spectroscopy
- Acknowledgements



Instrument for volumetric-densimetric measurements of binary coadsorption equilibria of gas mixtures on porous solids without using a gas chromatograph. The sorptive gas prepared in the system is assumed to be a binary mixture with known initial molar concentrations ( $y_1^*$ ,  $y_2^*$ ). © IFT University of Siegen, 2002.

Mass balances

$$m_i^a = m_i^* - m_i^f \quad i = 1, 2 \quad (1)$$

EOS

$$m_i^* = \frac{y_i^* p^* V_{SV}}{R T Z^*} M_i \quad Z = Z(p^*, T, y_i^*) \quad (2)$$

Sorptive gas masses  
( $m_1^f, m_2^f$ )

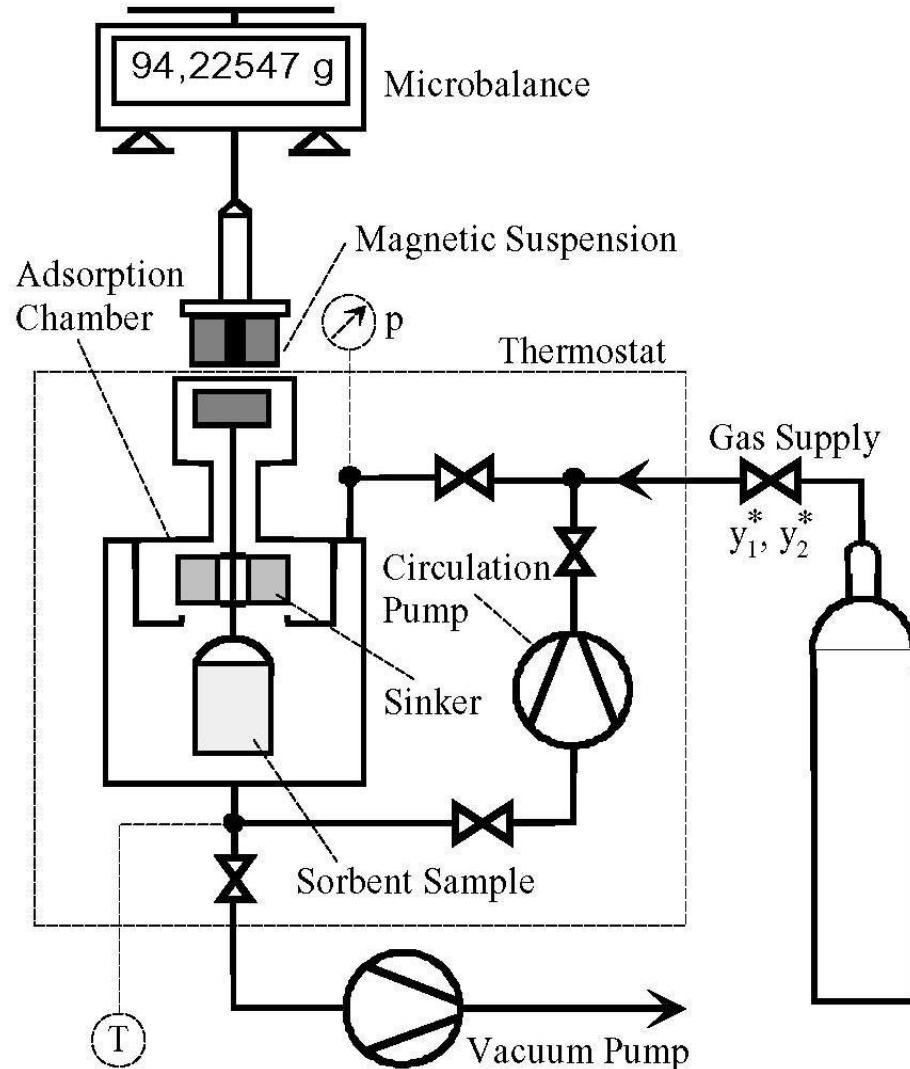
$$m_1^f + m_2^f = \rho^f V^* - V^{as} \quad (3)$$

$$\frac{m_1^f}{M_1} + \frac{m_2^f}{M_2} = \frac{p V^* - V^{as}}{R T Z(p, T, w_i)} \quad (4)$$

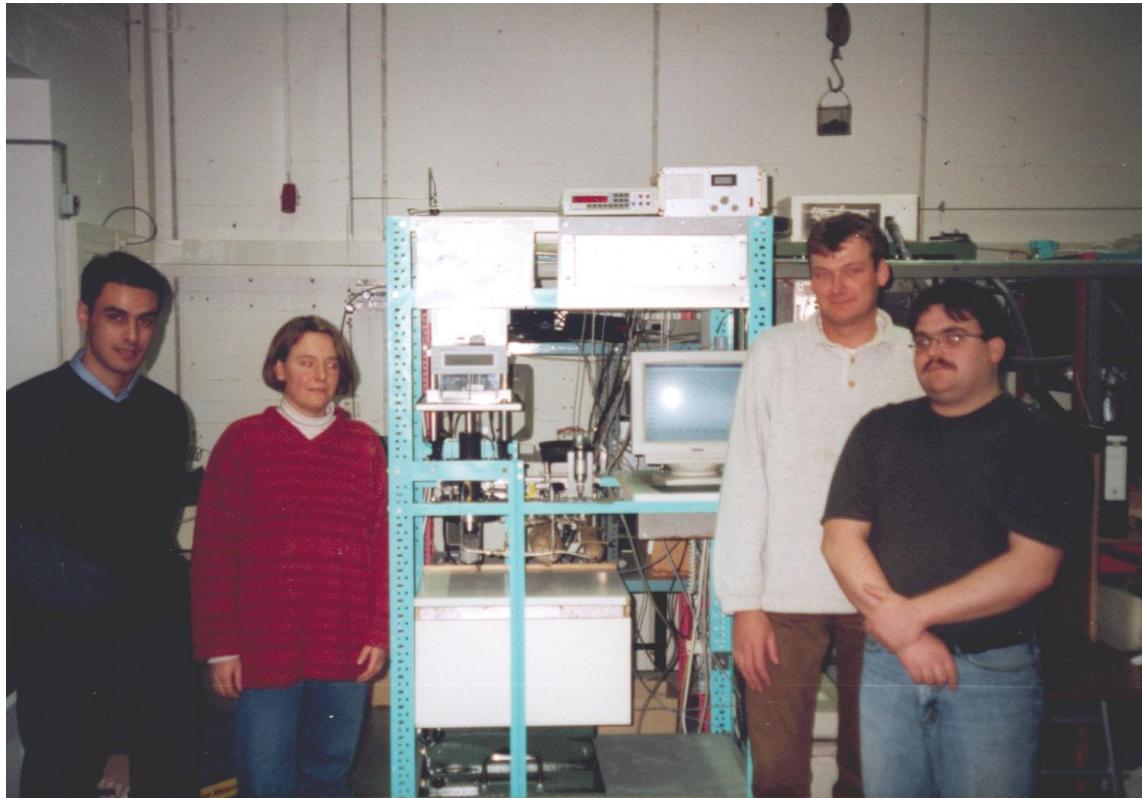
$$w_i = \frac{m_i^f}{m_1^f + m_2^f} \quad i = 1, 2$$

$$(1 - 4) \quad V^{as} = V_{He}^s \quad (5)$$

$$m_{iGE}^a = m_i^* - \frac{M_i}{M_i - M_{i+1}} \left( \rho^f - \frac{p M_{i+1}}{R T Z(p, T, w_i)} \right) V^* - V_{He}^s \quad (6)$$



## Installation for DGMs of Binary Coadsorption Equilibria of Premixed Gases ( $y_1^*$ , $y_2^*$ )



**First performance of DGMs using a MSB (3)  
on 1998-02-11 in Lab PB-A0126 of IFT/USI**

Mass balances     $m_i^a = m_i^* - m_i^f \quad i = 1, 2$       (1)

Total gas mass supplied     $m^* = m_1^* + m_2^* = m_1^a + m_2^a + m_1^f + m_2^f$       (2)

$$\begin{aligned} m^* &= \Omega + \rho^f V^* \\ m_i^* &= w_i^* m^* \end{aligned} \quad (2A)$$

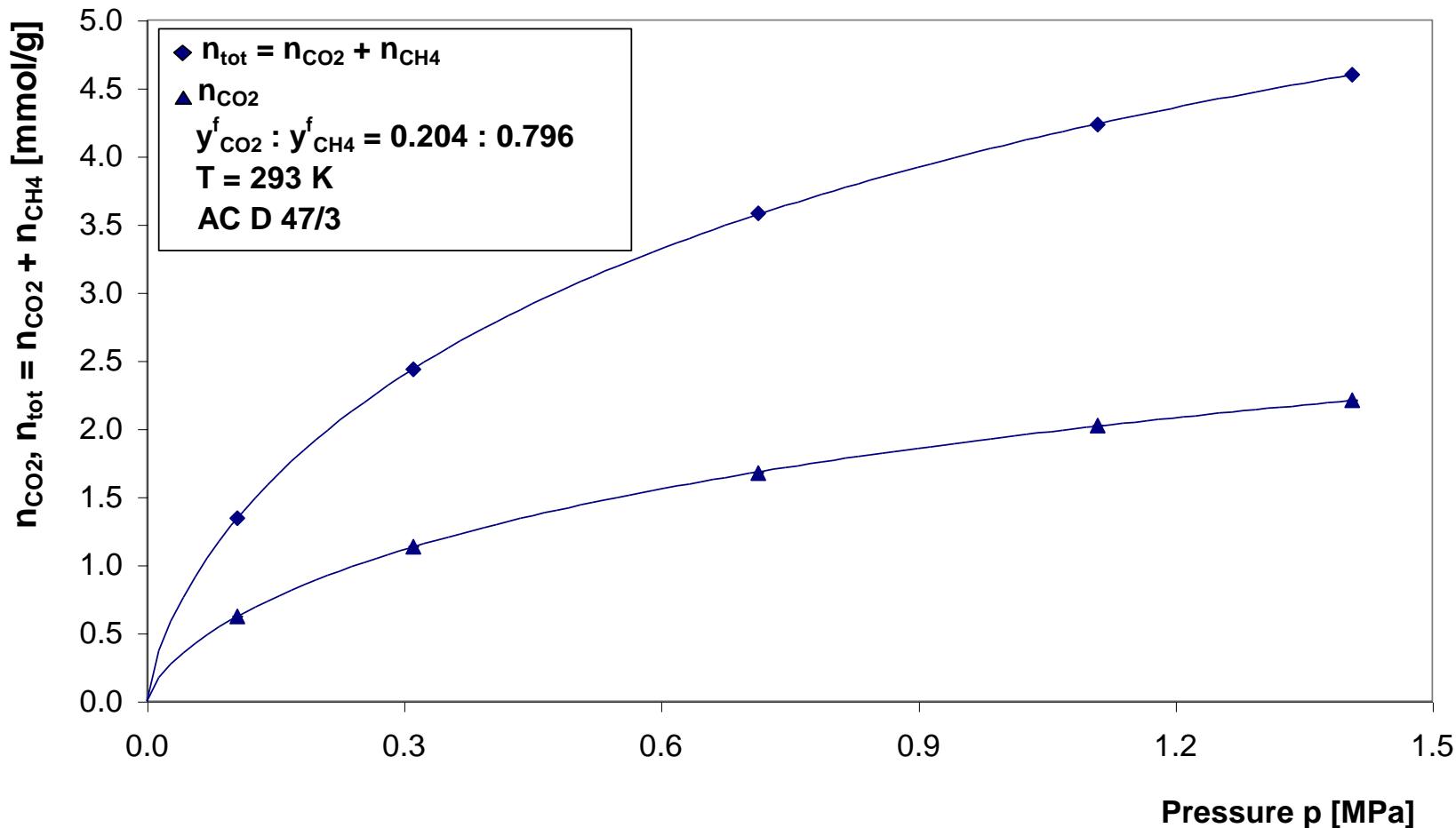
Sorptive gas masses     $m_1^f + m_2^f = \rho^f V^* - V^{as}$       (3)

$$\frac{m_1^f}{M_1} + \frac{m_2^f}{M_2} = \frac{p}{R T Z} \frac{V^* - V^{as}}{p, T, w_i} \quad (4)$$

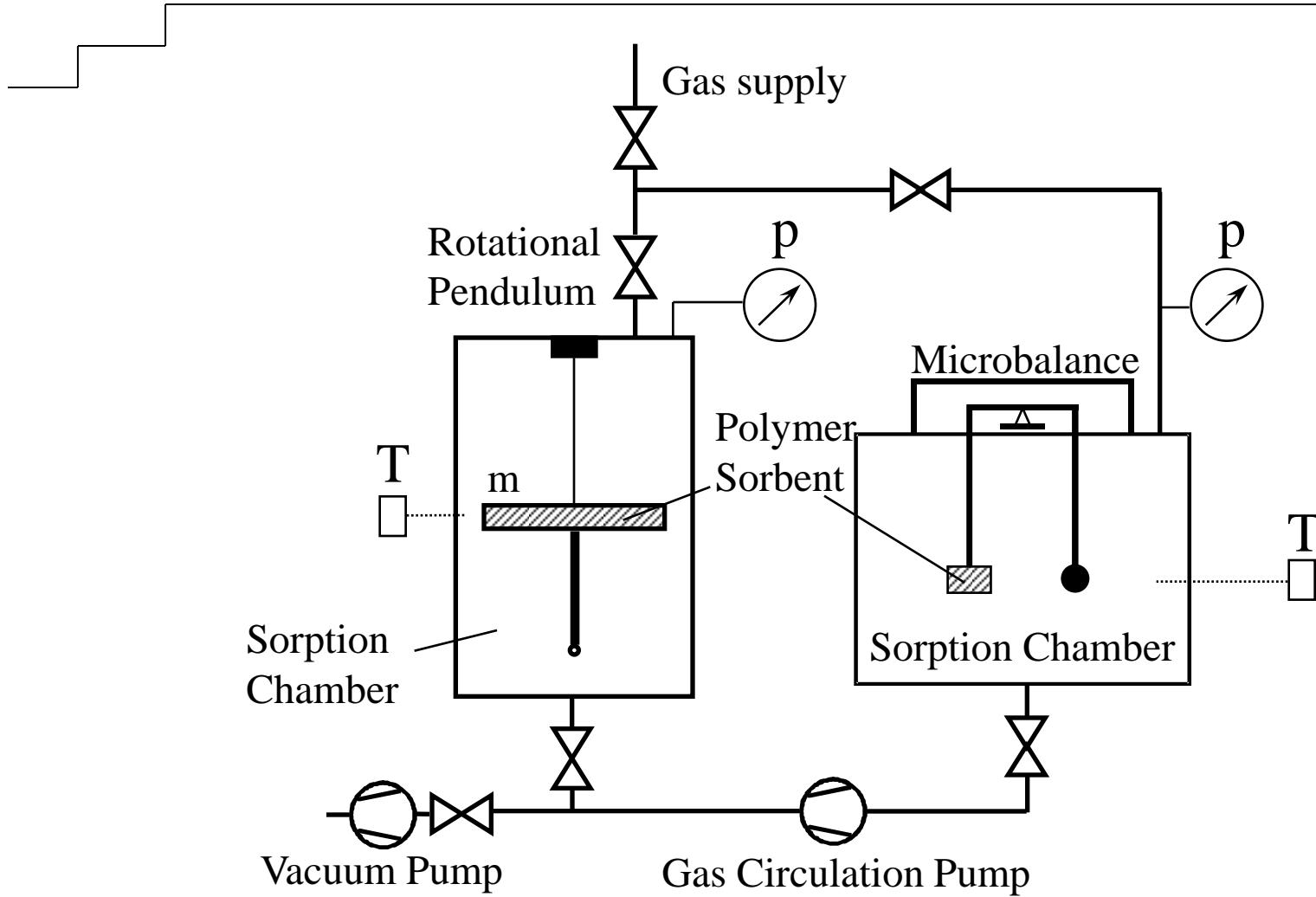
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(1, 2A, 3, 4)     $V^{as} = V_{He}^s$       (5)

$$m_{iGE}^a = m_i^* - \frac{M_i}{M_i - M_{i+1}} \left( \rho^f - \frac{p M_{i+1}}{R T Z p, T, w_i} \right) V^* - V_{He}^s \quad (6)$$



Coadsorption equilibria of  $\text{CO}_2 / \text{CH}_4$  at  $T = 293\text{K}$ ,  $y_{\text{CO}_2} = 20.4\% \text{ mol}$ ,  $y_{\text{CH}_4} = 79.6\% \text{ mol}$   
on AC D47/3. Correlation by GAI:  $n_i = n_{i_\infty} (\text{bp})^{\alpha_i} / [1 + (\text{bp})^{\alpha_i}]$ ,  $i = \text{CO}_2, \text{CH}_4$



## Experimental setup for oscillometric-gravimetric measurements

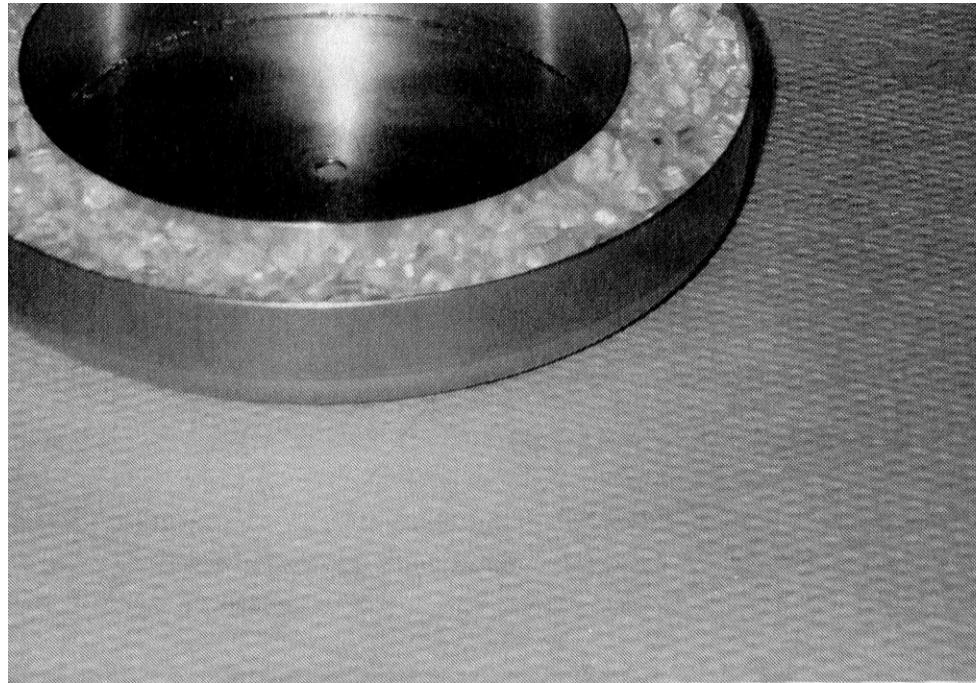
Ideal Pendulum  $m^s, m$ 

$$\frac{m}{m^s} = \frac{1 + \Delta_0^2}{1 + \Delta_E^2} \left( \frac{\omega_0}{\omega_E} \right)^2 - 1$$

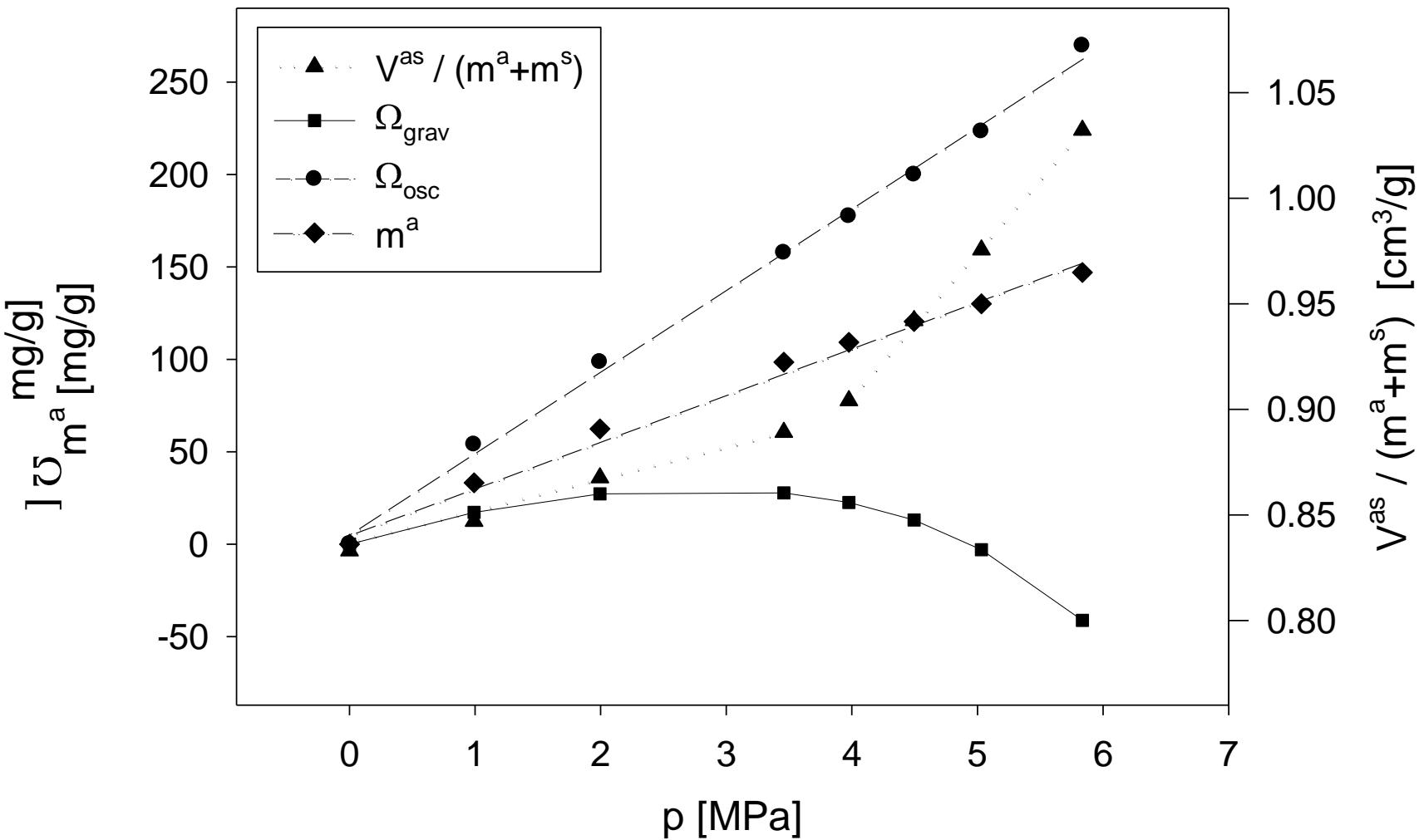
Physical Pendulum  $m^*, m^s, m$ 

$$\frac{m}{m^s} = \frac{\frac{1 + \Delta_0^2}{1 + \Delta_E^2} \left( \frac{\omega_0}{\omega_E} \right)^2 - 1}{1 - \frac{\Delta_0 \omega_0}{\Delta^* \omega^*}}$$

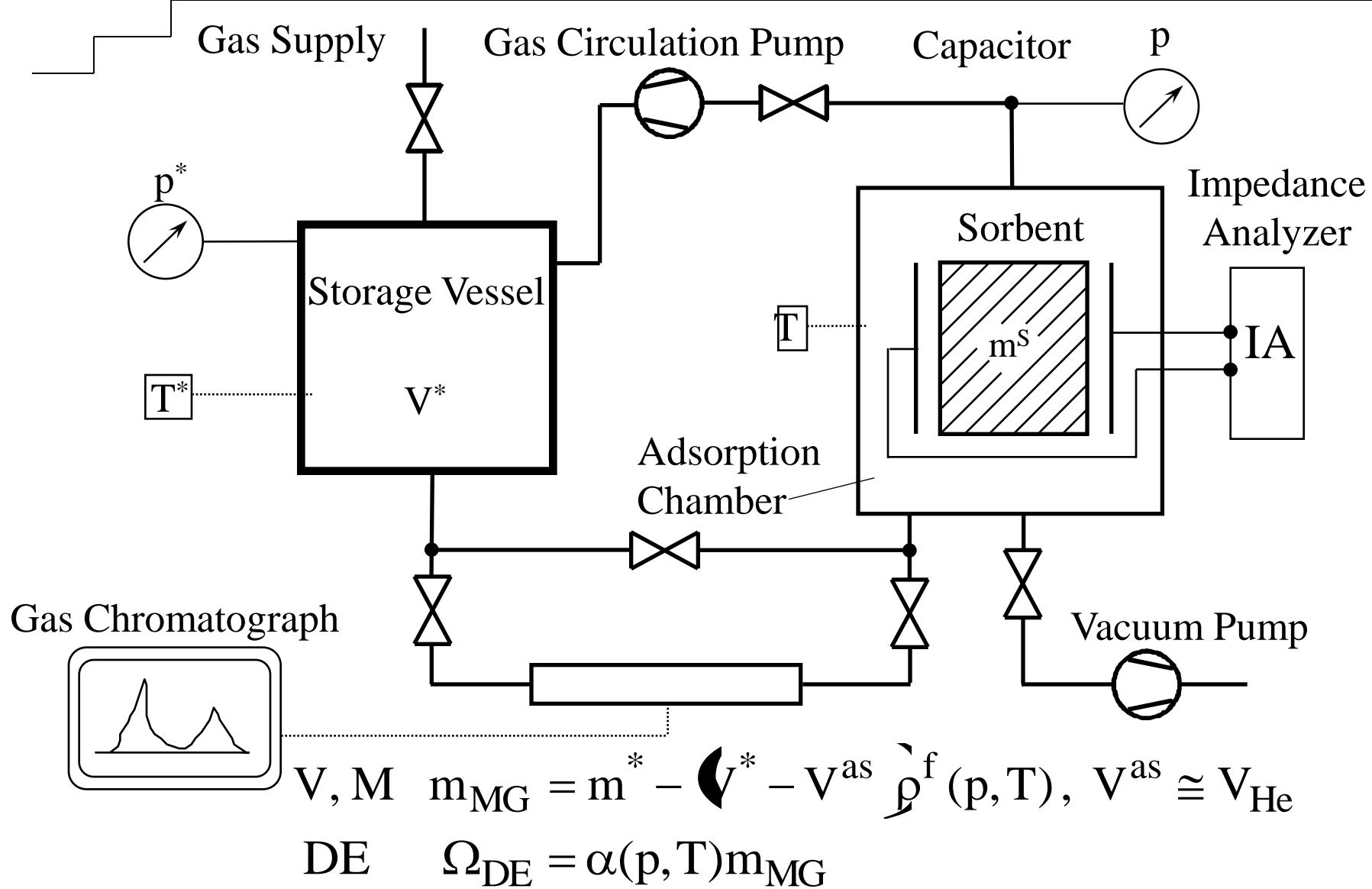
 $\omega^*, \Delta^*$  ... empty pendulum  $m^*$ , vacuum $\omega_0, \Delta_0$  ... pendulum and adsorbent  $m^*, m^s$ , vacuum $\omega_E, \Delta_E$  ... pendulum, adsorbent, adsorbate  $m^*, m^s, m$ , gas**Oscillometric measurements of gas adsorption equilibria. Theory**



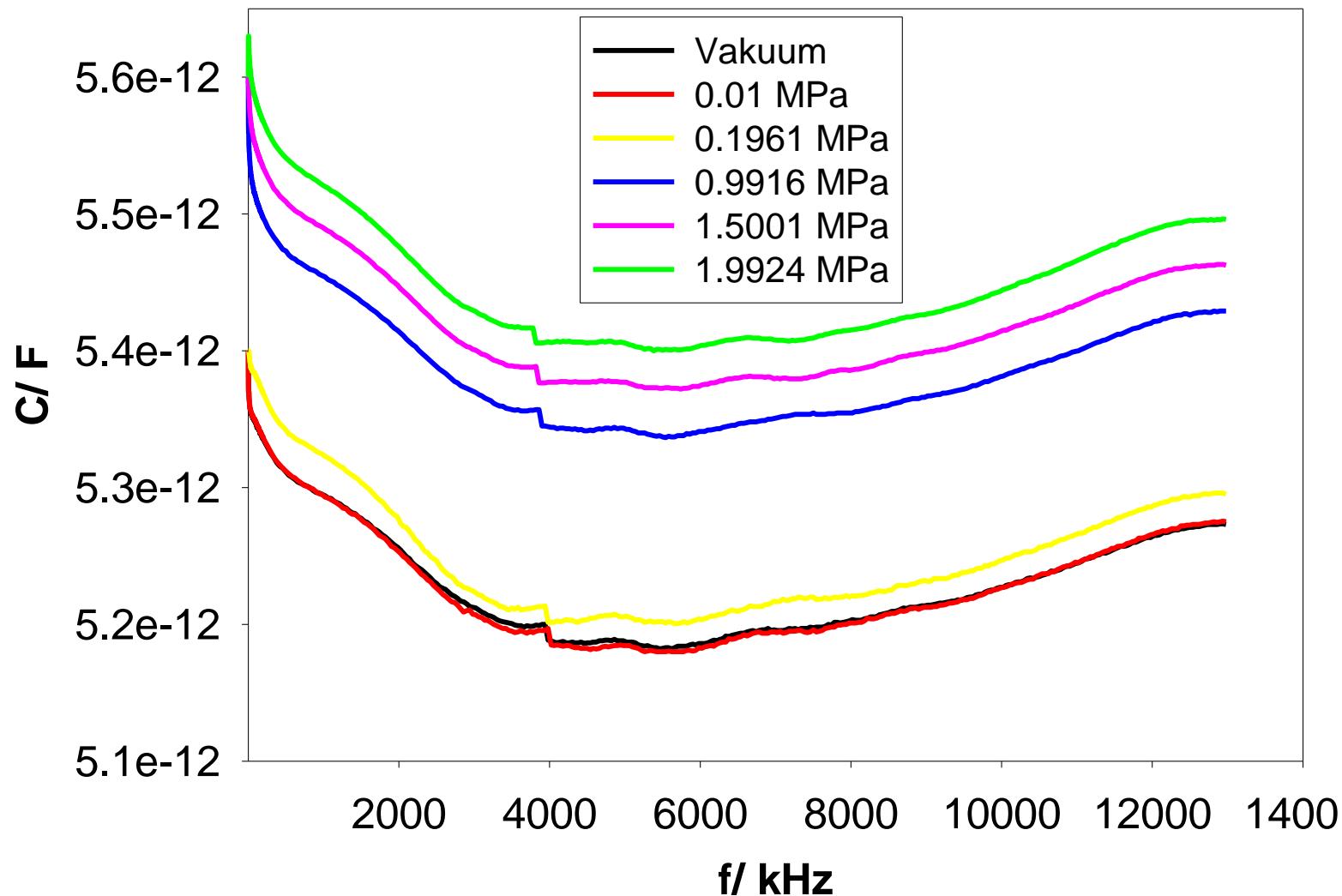
**Ring slit of rotational pendulum filled with polycarbonate pellets**



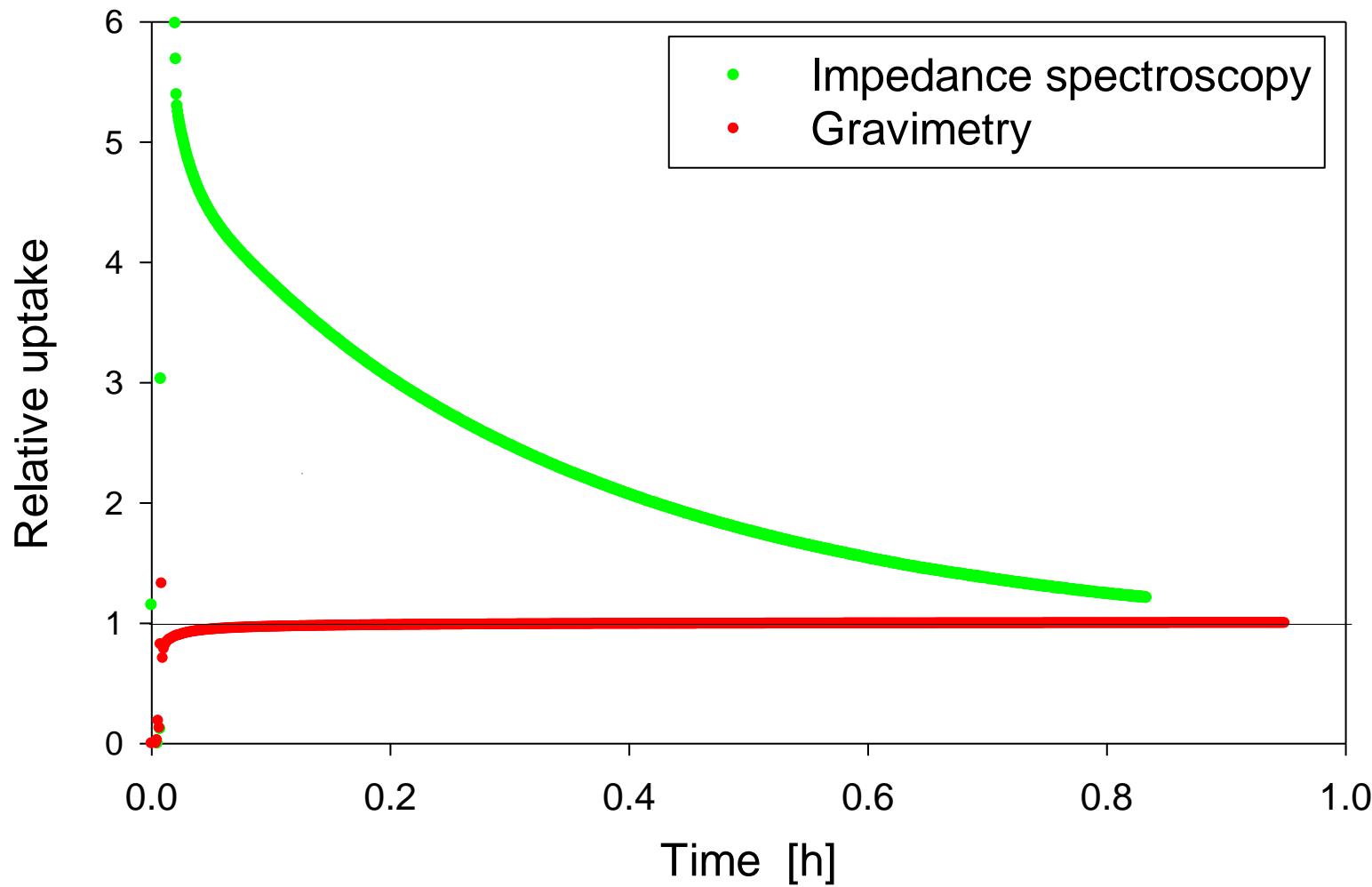
**Swelling and sorption isotherm of polycarbonate /  $\text{CO}_2$  at 293 K**



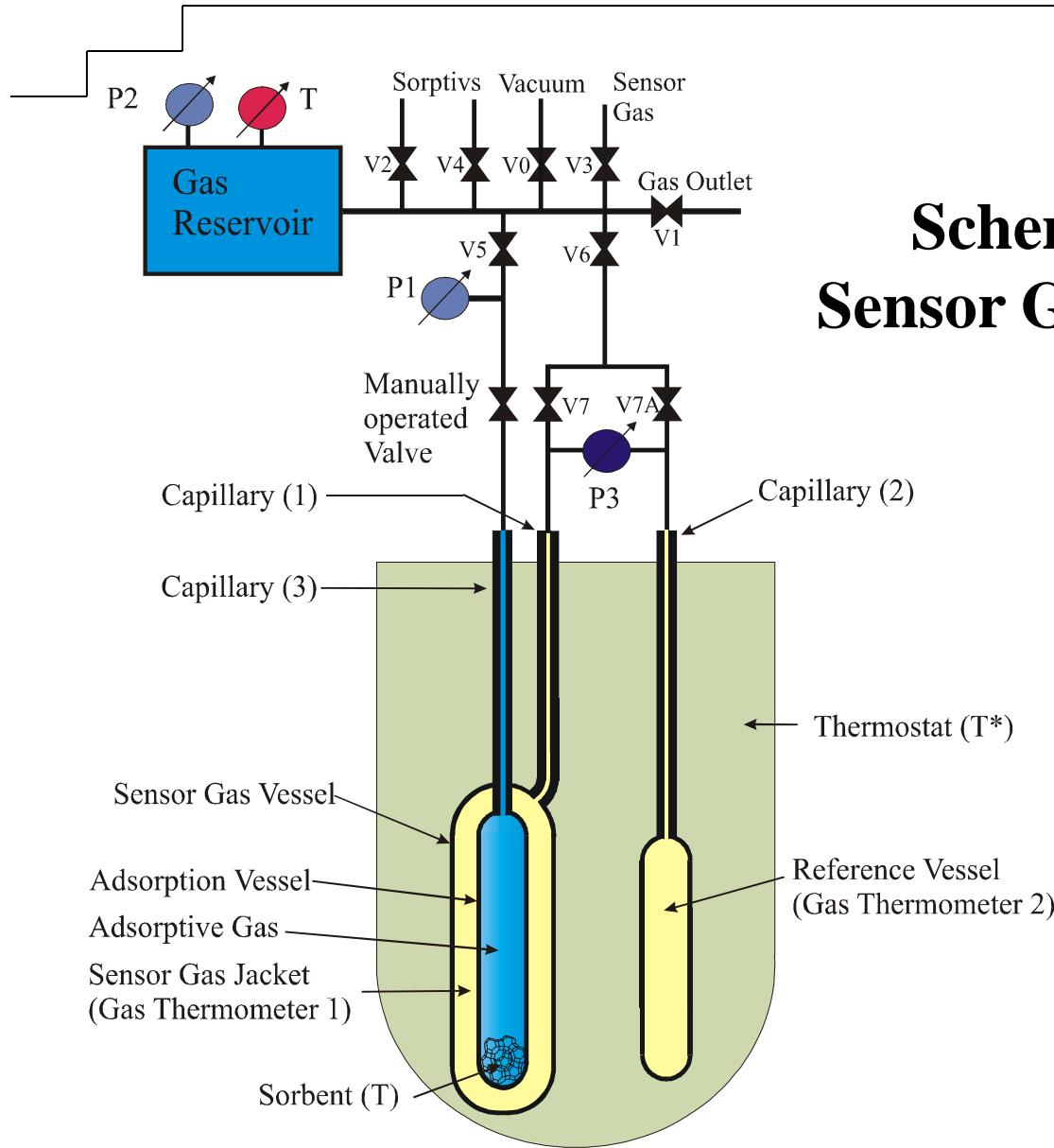
**Experimental setup for volumetric-dielectric measurements**



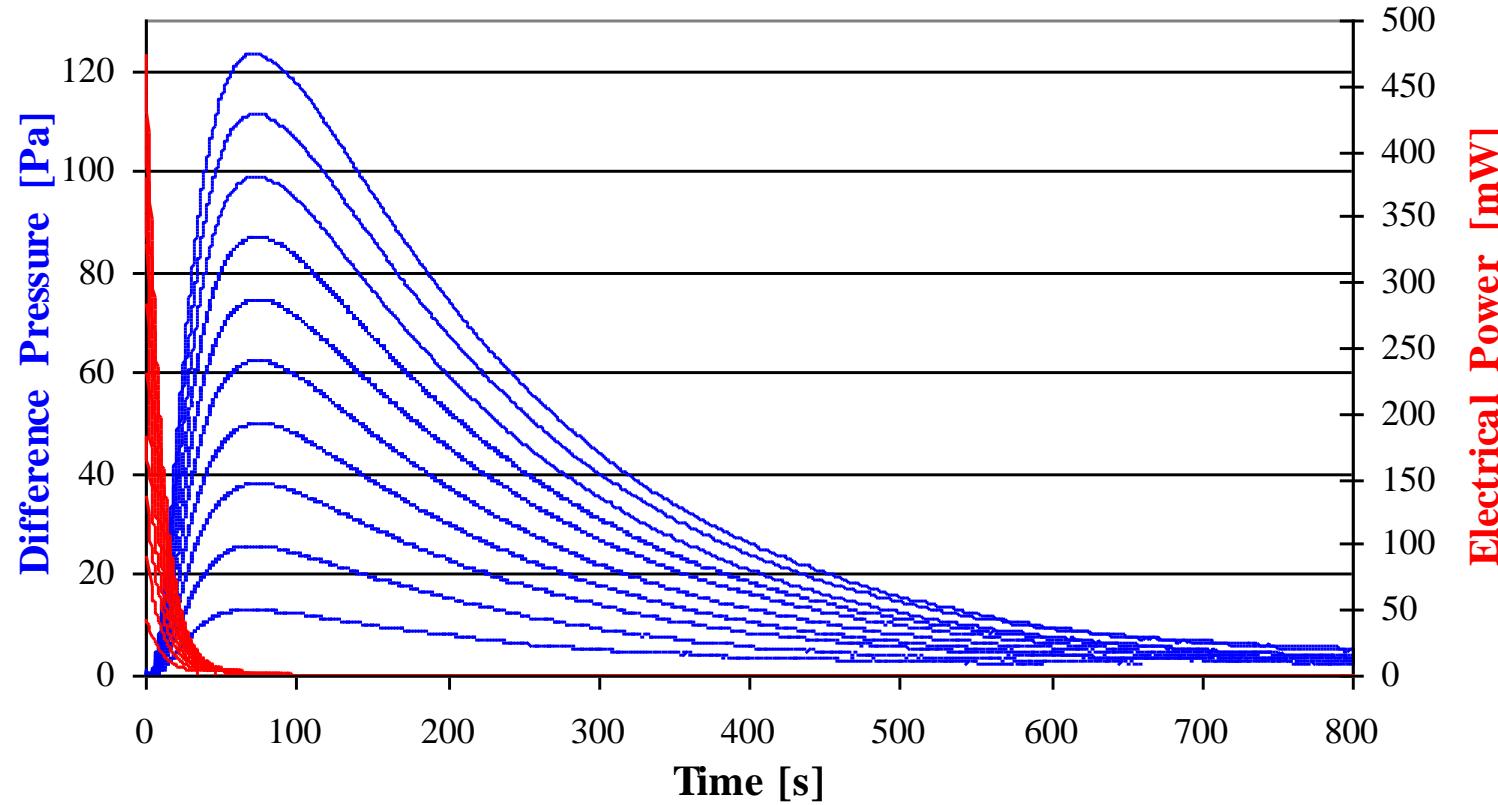
Impedance spectra of  $\text{CO}_2$  on zeolite (DAY),  $T=298\text{K}$



**Uptake curves of  $\text{H}_2\text{S}$  on MS 13X,  $T=298\text{K}$**

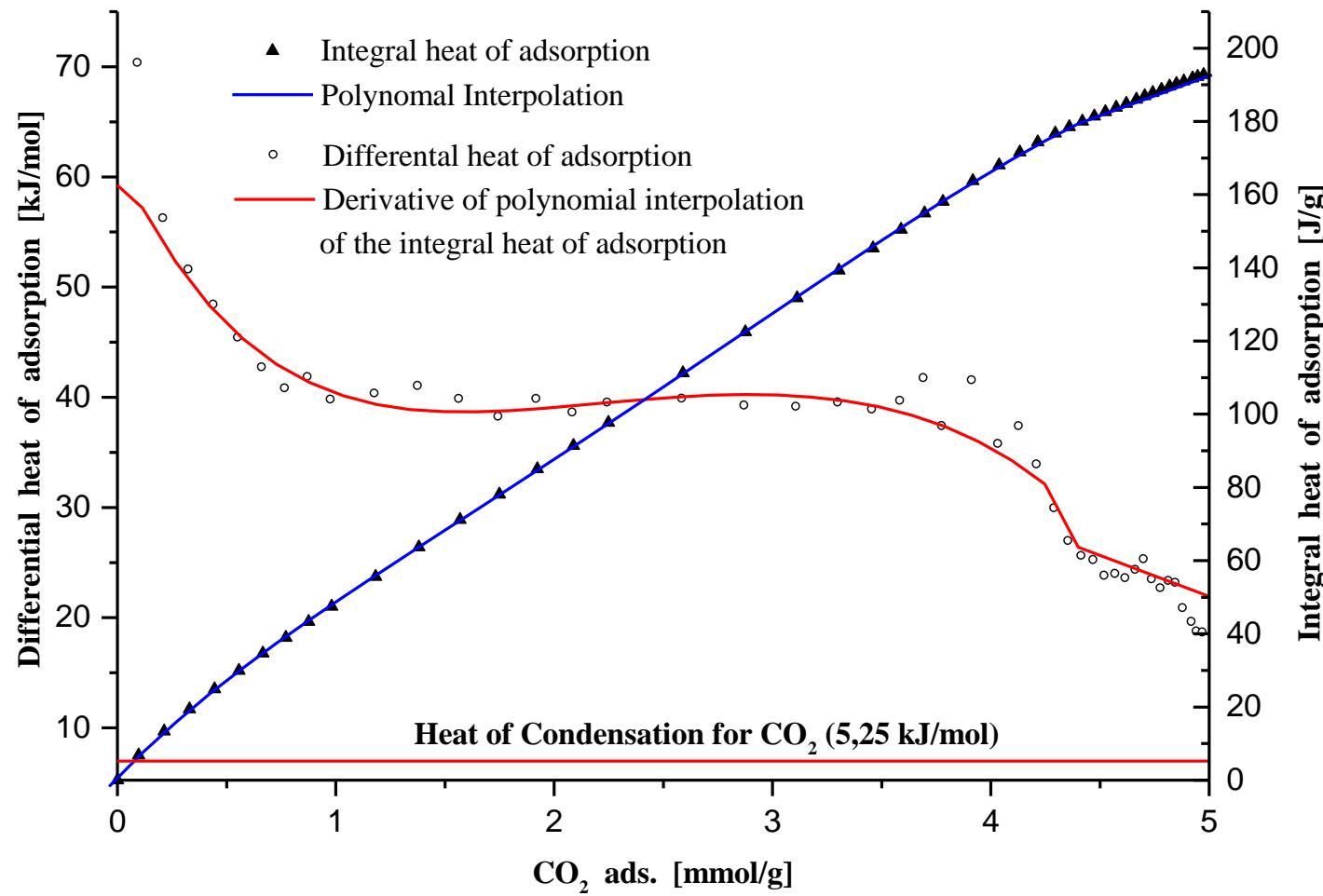


## Schematic diagram of a Sensor Gas Calorimeter (SGC)

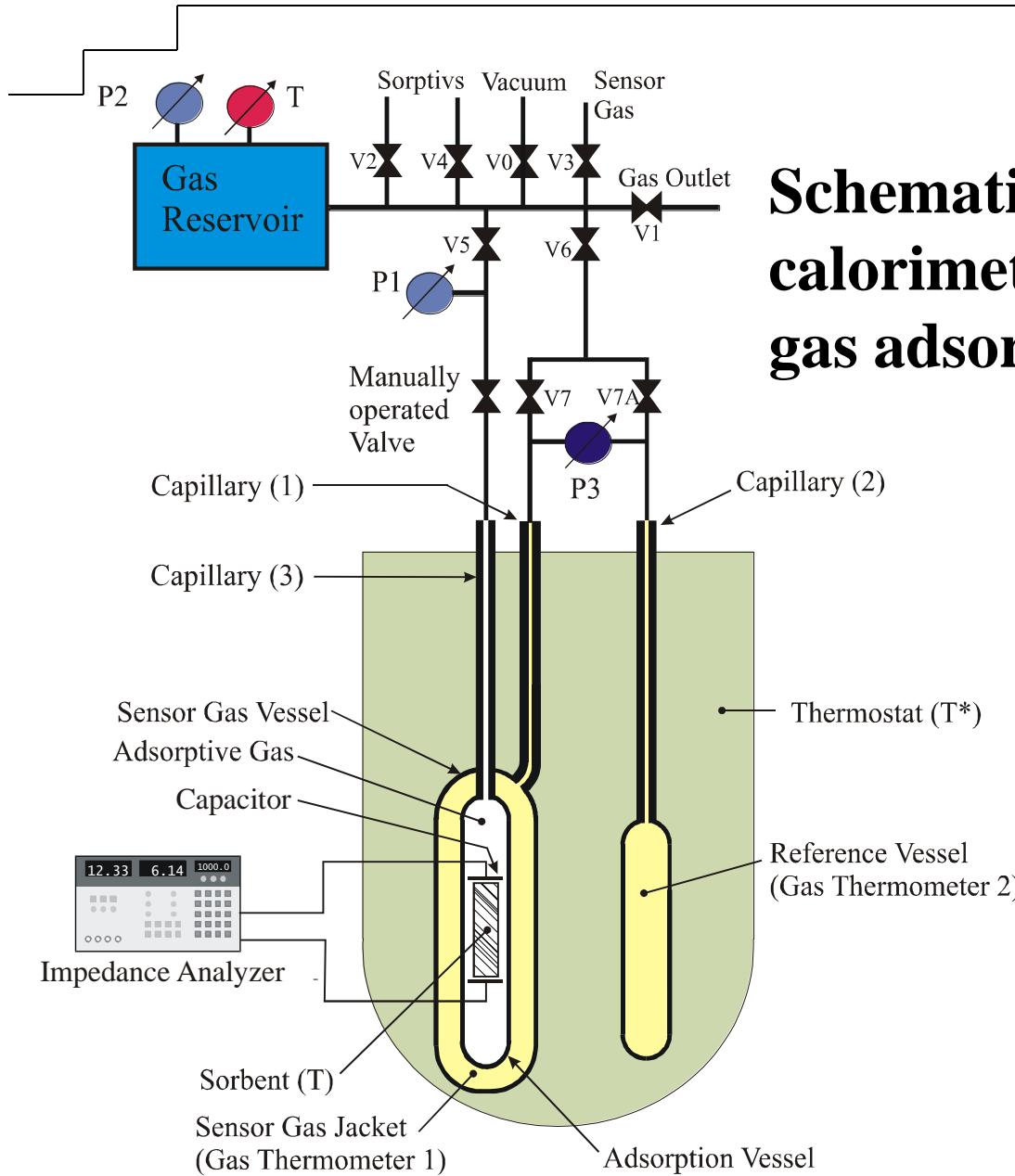


## Calibration experiments in the SGC 0.5J to 5J Sensor gas N<sub>2</sub> (1.6bar), T=298K, $\tau=10\text{s}$

Ohm's heat release (red lines) → Pressure signal (blue lines)



Heat of adsorption for  $\text{CO}_2 / \text{Na}13\text{X}$ , T=298K



## Schematics of combined calorimetric-dielectric-volumetric gas adsorption measurements

$$(CI) \quad h = h_0 + Be^{-bp}$$

$$\rightarrow \frac{H}{m} - h_0 = B \left( \frac{(\Pi/m) - \hat{\alpha}_0}{A} \right)^{b/a}$$

$$(DI) \quad \frac{\hat{\alpha} = \hat{\alpha}_0 + Ae^{-ap}}{}$$

$$\rightarrow h - h_0 = B \left( \frac{\hat{\alpha} - \hat{\alpha}_0}{A} \right)^{b/a}$$

$$h = \frac{H}{m}$$

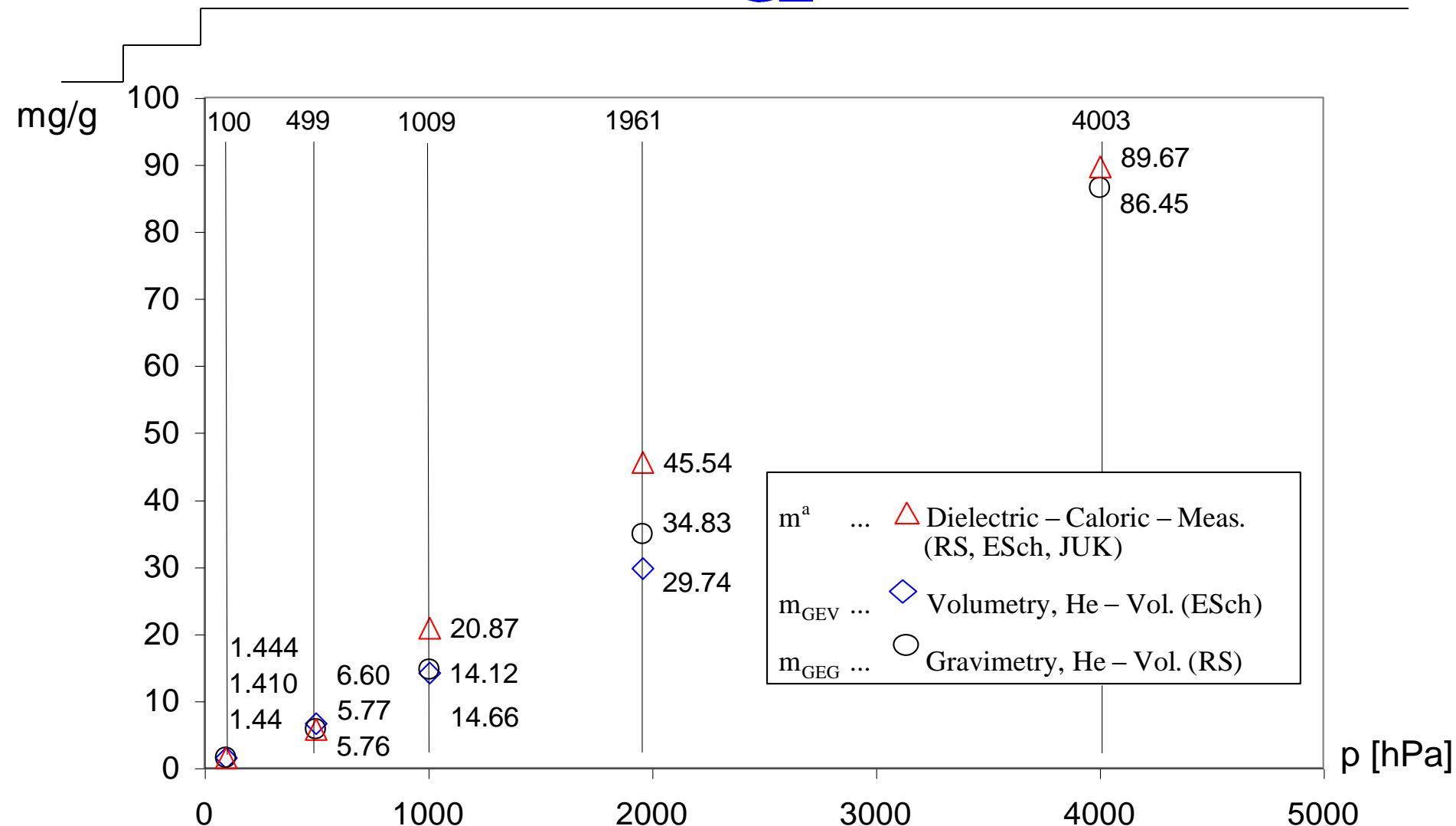
$$\hat{\alpha} = \frac{\Pi}{m}$$

$$m = H \sqrt{ \left[ h_0 + B \left( \frac{(\Pi/m) - \hat{\alpha}_0}{A} \right)^{b/a} \right] } \quad *)$$

$$\sum_i \left[ \frac{H - h}{B} \right]_i^2 +$$

$$\sum_k \left[ \frac{\Pi - \hat{\alpha}}{A} \right]_k^2 \rightarrow \text{Min}$$

$\rightarrow a, A, b, B \rightarrow (*) \rightarrow m$



Absolute masses ( $m^a$ ) and Gibbs excess masses ( $m_{GEV}$ ,  $m_{GEG}$ )  
of  $\text{CO}_2$  adsorbed on wessalite (DAY-zeolite) at  $T=298\text{K}$

# Gas Mixture Sorption

## Measurement Methods

	M	G	O	SP	CHR	D	C
Manometry (M)		++	+	0	++	++	0
Gravimetry (G)	2		+	0	+	+	0
Oscillometry (O)	1, V	1, V		0	0	0	0
Spectroscopy (SP)	(2)	(2)	1, V		-	-	AMA
Chromatography (CHR)	≥2	≥2	≥2*	-		-	-
Densimetry (D)	2	2	1, V	-	-		-
Calorimetry (C)	(1)	(1)	(1)	1	-	-	



**GVC-GET Thermodynamic-Conference Würzburg, 2001**